

Basic Science Department Math. I Code: Math 101 Final Exam: 5 / 1 / 2014 Time Allowed: 2 hours	 Modern University For Technology & Information Faculty of Engineering	Academic year: 2013 / 2014 Semester: Autumn Examiners: Dr. Mona Samir Dr. Mohamed Eid
Answer All Questions		Total Mark: 40

Question 1

Find y from the following:

- | | |
|--|--|
| (a) $y = 2x^4 + 4^x - 1$ | (b) $y = 4^{\sin x} + \tan^{-1} x^2$ |
| (c) $y = \cos x + x^{\cos x}$ | (d) $y = \cosh 3x \cdot \tanh^{-1} x^2$ |
| (e) $y \sec x + x \operatorname{sech} y = 1$ | (f) $y = t + \log t, \quad x = \sqrt{t} + \ln t$ |

10

Question 2

(a) Determine the maximum and minimum points of the function:

$$f(x) = 2x - e^{2x}$$

3

(b) Write the Taylor's expansion of the function: $f(x) = x \cos x$ at $x = \pi$.

3

Question 3

Find the following integrals:

12

- | | | |
|-------------------------------|---|---------------------------------------|
| (a) $\int (x^4 + e^{2x}) dx$ | (b) $\int \left(\frac{1}{x^4} + \frac{1}{x} + 4x \right) dx$ | (c) $\int (\cosh x + e^x \cosh x) dx$ |
| (d) $\int x \cdot \cos 2x dx$ | (e) $\int \frac{x}{x^2 - 4x + 3} dx$ | (f) $\int \sin 3x \cdot \cos x dx$ |

Question 4

(a) Find the integral: $\int \cos^5 x dx$

4

(b) Find the area of the region between the curve $y = x^3 - x$, x-axis, x in $[-1, 1]$

4

(c) If the region between the curve $f(x) = 2^x$, x-axis, x in $[1, 2]$, is rotated

4

about: (i) x-axis (ii) y-axis.

Compute the volume of the generated solids.

Good luck

Dr. Mona Samir

Dr. Mohamed Eid

Engineering Mathematics Department Math. 1 Code: Math 101 Mid-Term Exam Time Allowed: 60 Minuets Answer All Questions	 Faculty of Engineering	Academic year: 2013 / 2014 Semester: Autumn Date: 24 / 11 / 2013 Examiners: Dr. Mona Samir Dr. Mohamed Eid Total Mark: 30
[1] Find y where:		12
(a) $y = 2x^3 + e^x + 4$	(b) $y = 7^{x^2} + \sin^{-1} x^3$	
(c) $y = \log x + \ln(x + \sin x)$	(d) $y = \cos 3x \cdot \sinh^{-1} x^2$	
(e) $y^3 = \sin(xy) + \ln(\cosh x + \cos x)$		
(f) $y = \tan t + \sec t, \quad x = \tanh t + \operatorname{sech} t$		
[2] Find the integrals:		6
(a) $\int (x^3 + 3^x + \ln 3) dx$	(b) $\int (\frac{1}{x^4} + \frac{1}{4^x} + 4x) dx$	(c) $\int (x^2 + 3)^2 dx$
[3] Find the following limits:		4
(a) $\lim_{x \rightarrow 0} \frac{\tan x}{3^x - 1}$	(b) $\lim_{x \rightarrow 1} \frac{x^3 - 3x^2 + 3x - 1}{x^3 - 2x^2 + x}$	
[4] Determine the maximum and minimum points of: $f(x) = x - 2 \ln x$		4
[5] Write the Taylor's expansion of the function: $f(x) = \ln x$ at $x = 1$.		4

Good luck

Dr. Mona Samir

Dr. Mohamed Eid

I	ID:	الاسم:
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(1) Find the integrals: (a) $\int \ln x \, dx$ (b) $\int x \sin x \, dx$ (c) $\int \sin^{-1} x \, dx$

(2) Find the area of region bounded by $y = x^2 - 2x$, x-axis, x in $[0, 3]$

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Answer

II	ID:	الاسم:
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- (1) Find the integrals: (a) $\int \log x \, dx$ (b) $\int x \cdot 4^x \, dx$ (c) $\int \sinh^{-1} x \, dx$
- (2) Find the volume V_y of the solid generated by rotating the region between $y = \frac{1}{1+x^2}$, x-axis, x in [1, 2] about y-axis.
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Answer

III	ID:	الاسم:
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(1) Find the integrals: (a) $\int x \ln x dx$ (b) $\int x \cdot \cos x dx$ (c) $\int \tanh^{-1} x dx$

(2) Find the volume V_y of the solid generated by rotating the region between:

$y = x + e^x$, x-axis, x in $[0, 1]$ about x-axis.

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Answer

IV	ID:	الاسم:
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(1) Find the integrals: (a) $\int x^2 \ln x \, dx$ (b) $\int x \sinh x \, dx$ (c) $\int \tanh^{-1} x \, dx$

(2) Find the area of region bounded by $y = 4 - x^2$, x-axis, x in $[1, 3]$

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Answer

G4	Sec:	ID:	Name:
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Find y' , where

$$(1) y = 3^x + 2 \cos x^3 + \sec x$$

$$(2) y = x^3 \cdot \log x + \ln(2x + \sin x)$$

$$(3) y = 5 + (2x + 2^x)^6$$

$$(4) y = 3^{\tan x} + \log_3(x + 2)$$

$$(5) y = \frac{\sin x}{x + \ln x}$$

$$(6) y = 3x + \tanh^{-1} 3x$$

$$(7) y = x + 3^x + \cos y$$

$$(8) y = 2^t + \cos 2t, \quad x = t^4 + \tanh 3t$$

G4	Sec:	ID:	Name:
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Find y' , where

$$(1) y = 3 \sin x^2 - \log(x + \sin x)$$

$$(2) y = 3^x \cdot x^3 + \ln x$$

$$(3) y = 3 + (x + \cos x)^5$$

$$(4) y = \left(\frac{3}{5}\right)^x + \frac{\ln x}{4} + \tan^{-1} x^3$$

$$(5) y = \frac{\log x}{3+\cos x}$$

$$(6) y = x - 2 \sinh x + \tan 3x$$

$$(7) y = x + \log x + \sinh y$$

$$(8) y = \sqrt{t} + \cosh 2t, \quad x = t^4 + \ln t$$

G5	Sec: A	ID:	Name:
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Find y' , where

$$(1) y = 3^x + 3x^2 + \sin 2x$$

$$(2) y = \sinh x \cdot \ln x + \cosh 3x$$

$$(3) y = (\log x + \sec x)^5$$

$$(4) y = 2^{x^3} + \sin^{-1} x^2$$

$$(5) y = \frac{2+\ln x}{2x+\sin x}$$

$$(6) y = \tan^{-1} x + \sinh^{-1} x^2$$

$$(7) y = x \sin x + \cos y$$

$$(8) y = t^3 + \cos 2t, \quad x = 3^t + \operatorname{sech} 3t$$

G5	Sec: B	ID:	Name:
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Find y' , where

$$(1) y = 3^x + \log x + \tan 2x$$

$$(2) y = \sinh x \cdot x^4 + \ln^4 x$$

$$(3) y = 8 \log 3 + x + \cos^4 x$$

$$(4) y = 2^{x^4} + \tanh^{-1} x^2$$

$$(5) y = \frac{x + \tanh x}{2x + \sin x}$$

$$(6) y = \tanh^{-1} x + \ln(x^2 + 3)$$

$$(7) y = x \ln x + \sin 2y$$

$$(8) y = \sqrt{t} + \cosh 2t, \quad x = e^t + \log 3t$$

G5	Sec: C	ID:	Name:
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Find y' , where

$$(1) y = e^x \cdot \log x + \tanh 2x$$

$$(2) y = \sinh x + x^4 + \log^4(x + 3)$$

$$(3) y = 8 \log x + \tan^4 x$$

$$(4) y = 2^{\sqrt{x}} + \sinh^{-1} x^2$$

$$(5) y = (\sin 3x + \log x)^8$$

$$(6) y = \tan^{-1} x + \ln(x^2 + \sinh x)$$

$$(7) y = x \tan x + \ln y$$

$$(8) y = \sqrt{t} + \cos 3t, \quad x = 4^t \cdot \log t$$